

55 (a) The salary of the first employee at the beginning of the n th year is given by

$$a_n = 30,000 + (n - 1)(2000) = 2000n + 28,000.$$

This is an arithmetic sequence with $a_1 = 30,000$ and $d = 2000$.

(b) The salary of the second employee at the beginning of the n th year is given by

$$b_n = 30,000(1.05)^{n-1}$$

This is a geometric sequence with $a_1 = 30,000$ and $d = 1.05$.

(c) At the beginning of the 10th year each salary is

$$a_{10} = 2000(10) + 28,000 = \$48,000,$$

$$b_{10} = 30,000(1.05)^{10-1} \approx \$46,540.$$

At the beginning of the 20th year the salaries are

$$a_{20} = 2000(20) + 28,000 = \$68,000,$$

$$b_{20} = 30,000(1.05)^{20-1} \approx \$75,809.$$

(d) The graph of each sequence is shown in *Figure 55*. With time the geometric sequence overtakes the arithmetic sequence, since $r > 1$.

$[0, 30, 10]$ by $[0, 150,000, 50,000]$

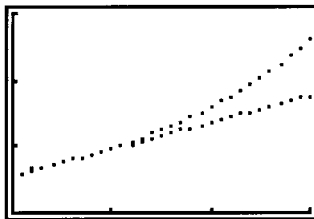


Figure 55